



# Mapping a pixel using kernel regression

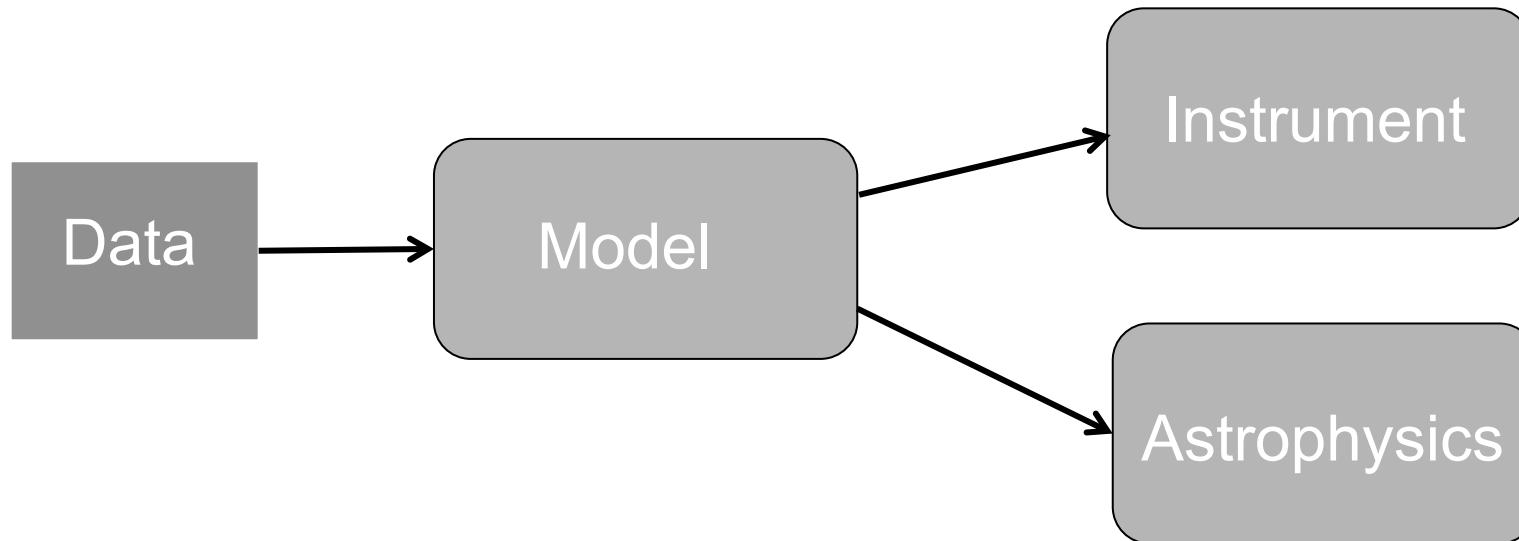
**Jim Ingalls**

**Jessica Krick, Sean Carey, Carl Grillmair  
(Spitzer Science Center)**

# Goal



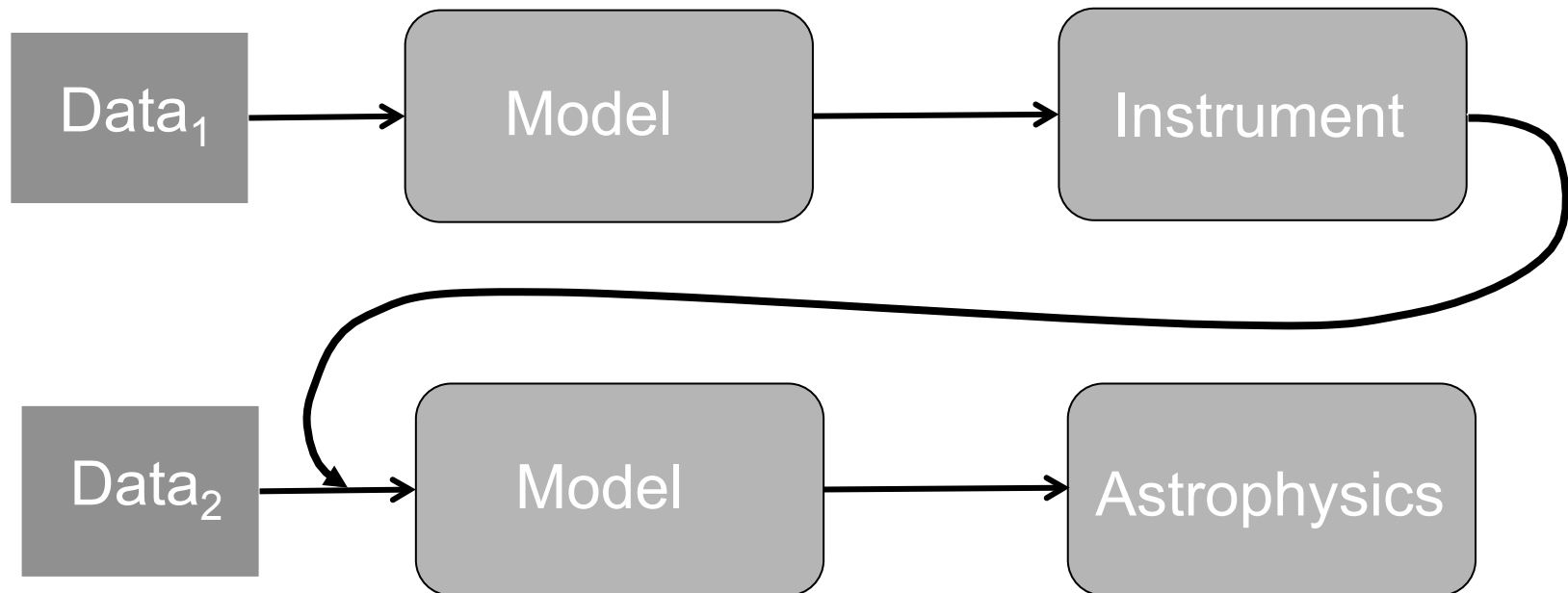
Develop a correction for correlated noise in IRAC photometry, that is independent of the data to be corrected



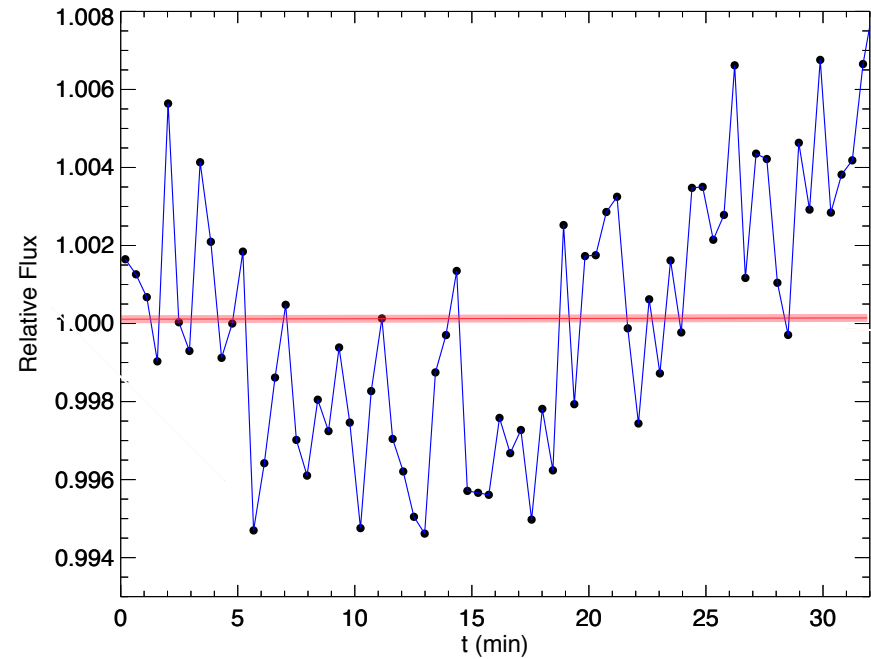
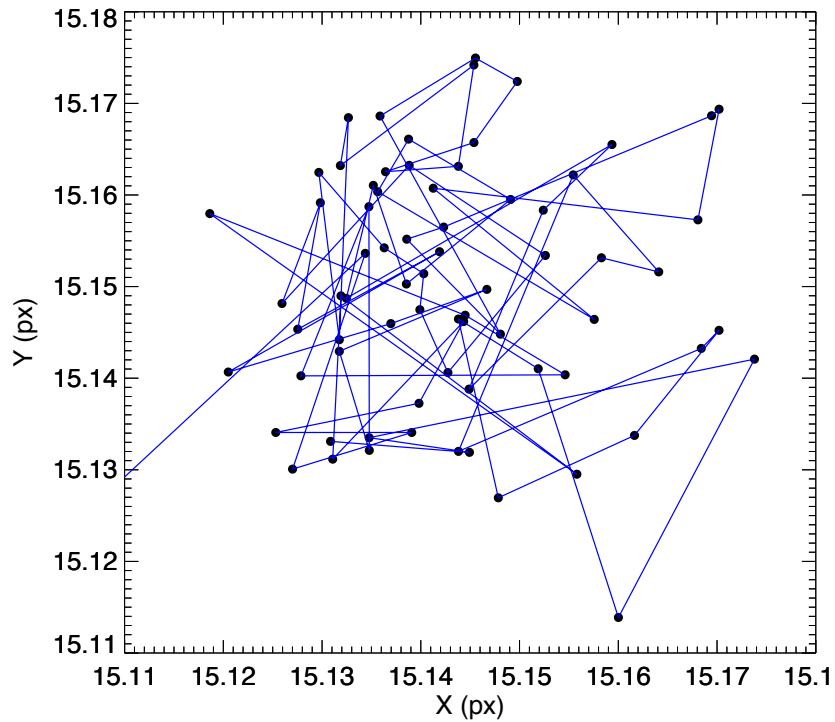
# Goal



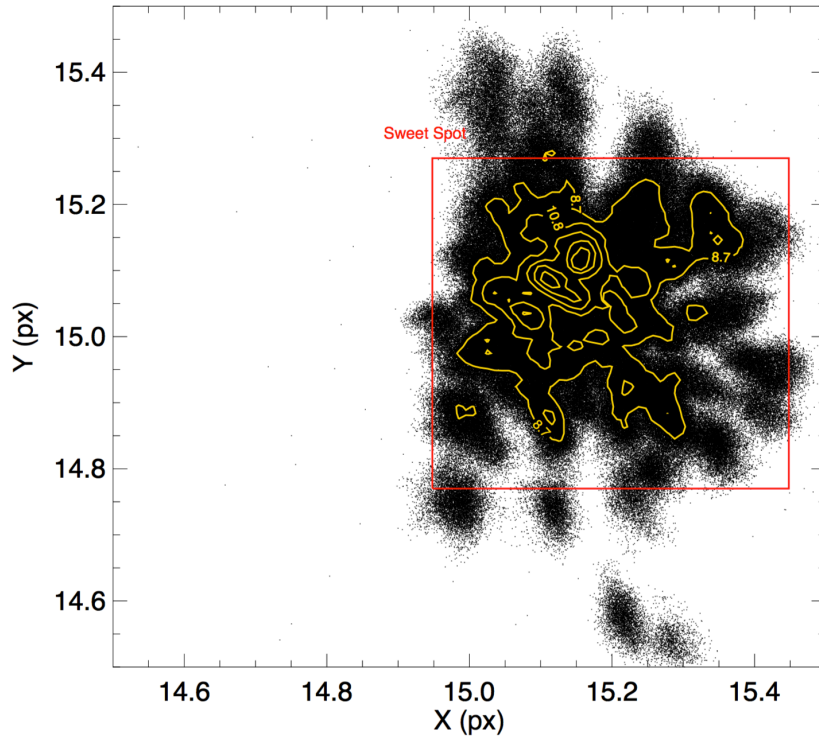
Develop a correction for correlated noise in IRAC photometry, that is independent of the data to be corrected



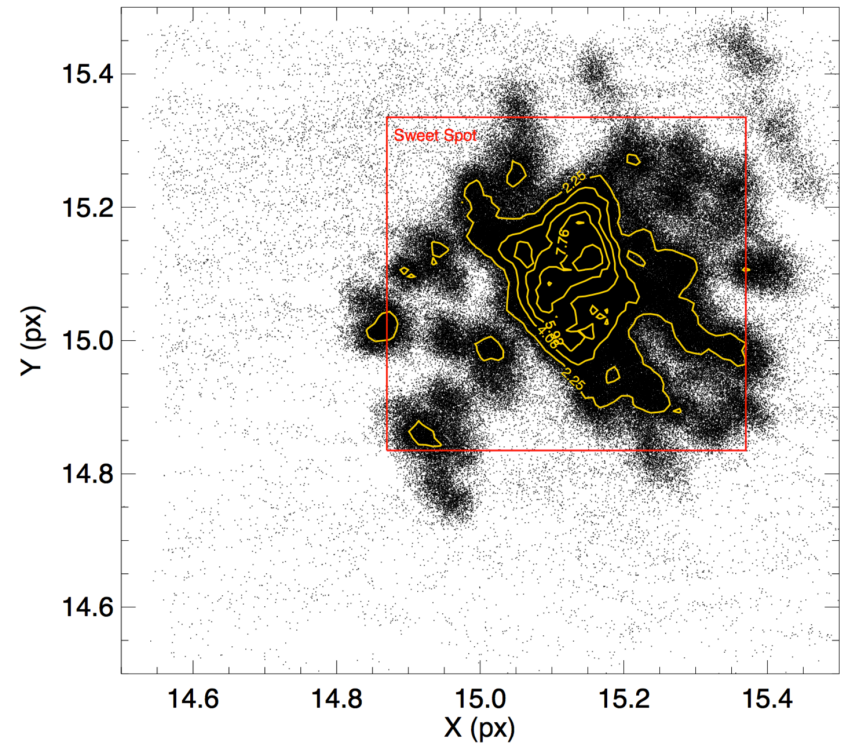
# Correlated Noise in IRAC photometry



# Mapping the Intrapixel Gain



Channel 1: 800,000  
measurements  
KF09T1



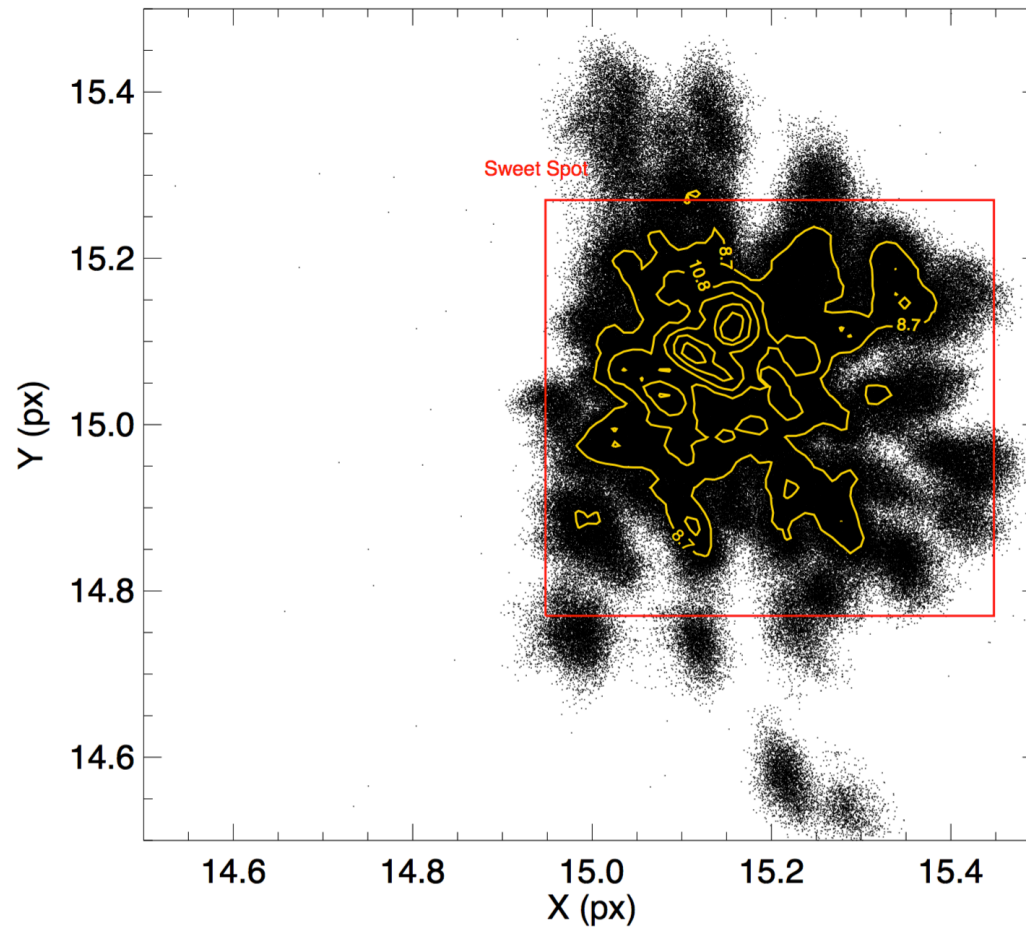
Channel 2: 500,000  
measurements  
BD+67 1044

$$\overline{F}(x, y) = \frac{\sum_{i <} f_i K_i}{\sum_{i <} K_i}$$

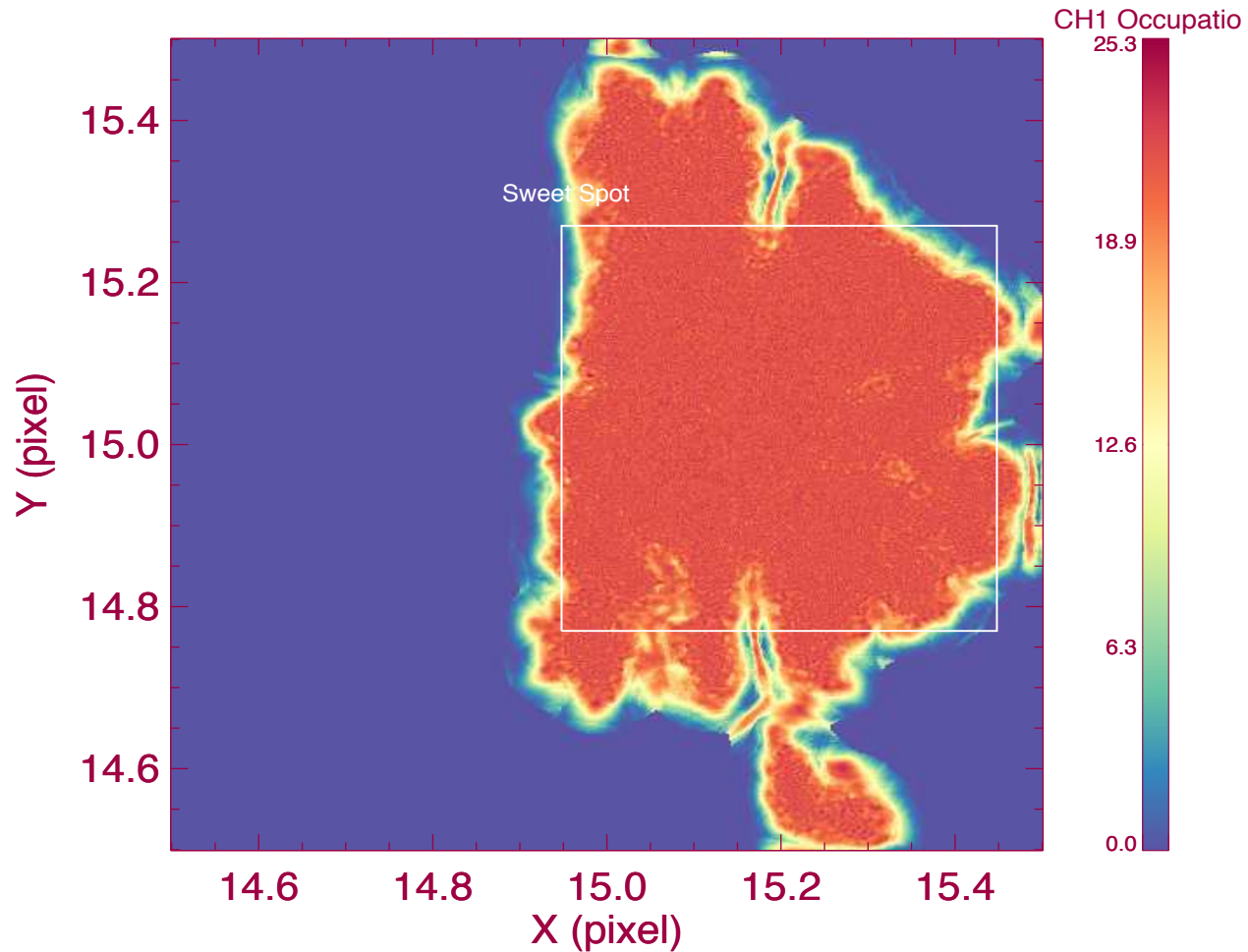
- Non-parametric regression – an inverse-distance weighted mean of the data around a point (x,y)
- Ballard et al. (2010), with science data
- Sum over ~100 nearest neighbors
- Gaussian kernel “occupation”, width given by nearest neighbors’ std. dev. in (x,y).
- Kernel can accept Noise Pixels, or (x,y) FWHM

$$K_i(x, y) = O_i(x, y) / \sigma^2(f_i) \quad O_i(x, y) \equiv \exp \left\{ - \left[ \frac{(x - x_i)^2}{2\delta_x^2} + \frac{(y - y_i)^2}{2\delta_y^2} \right] \right\}$$

# Mapping a Pixel: CH1



# Mapping a Pixel: CH1

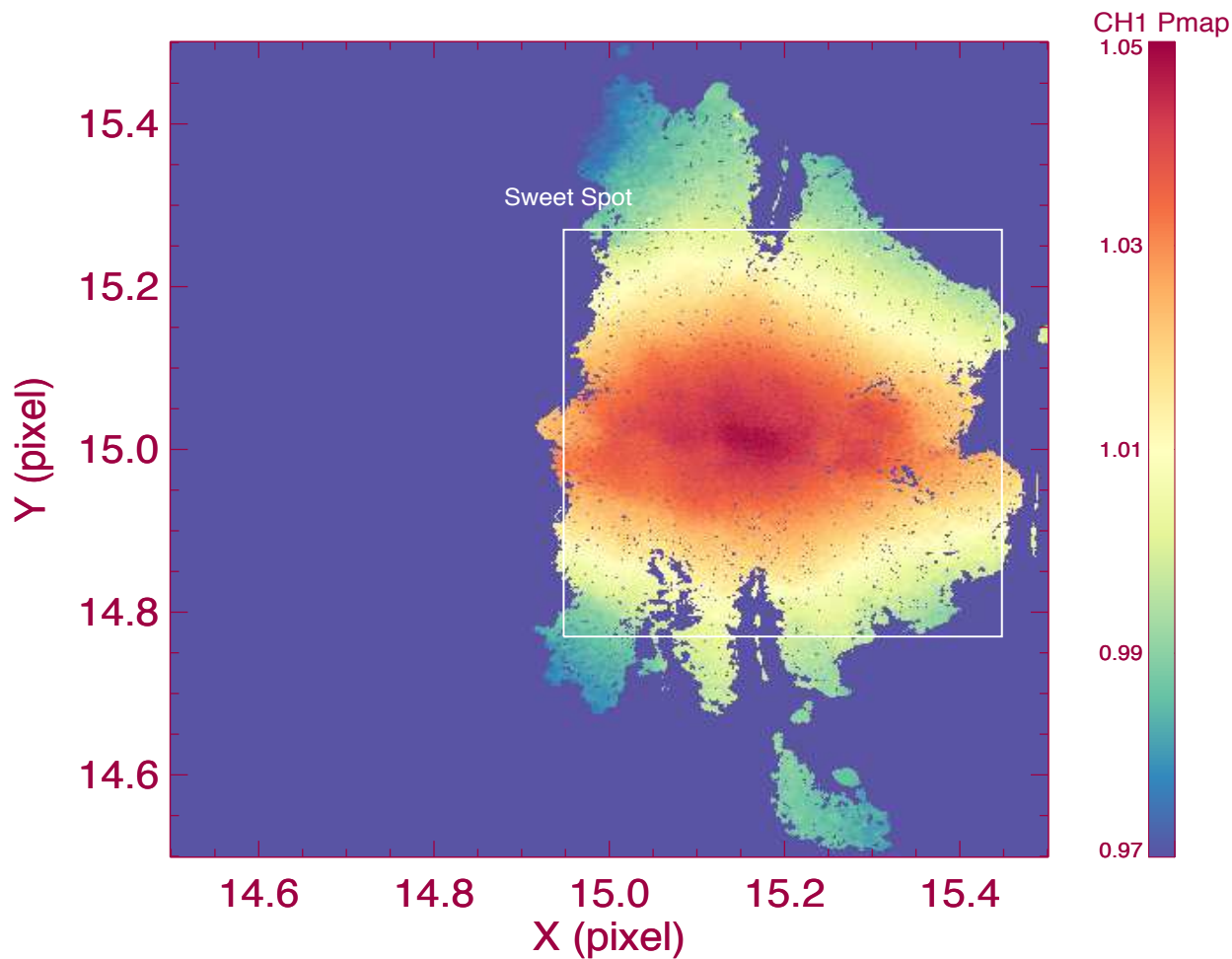


$$O_i(x, y) \equiv \exp \left\{ - \left[ \frac{(x - x_i)^2}{2\delta_x^2} + \frac{(y - y_i)^2}{2\delta_y^2} \right] \right\}$$

$$O(x, y) = \sum_{i <} O_i(x, y)$$

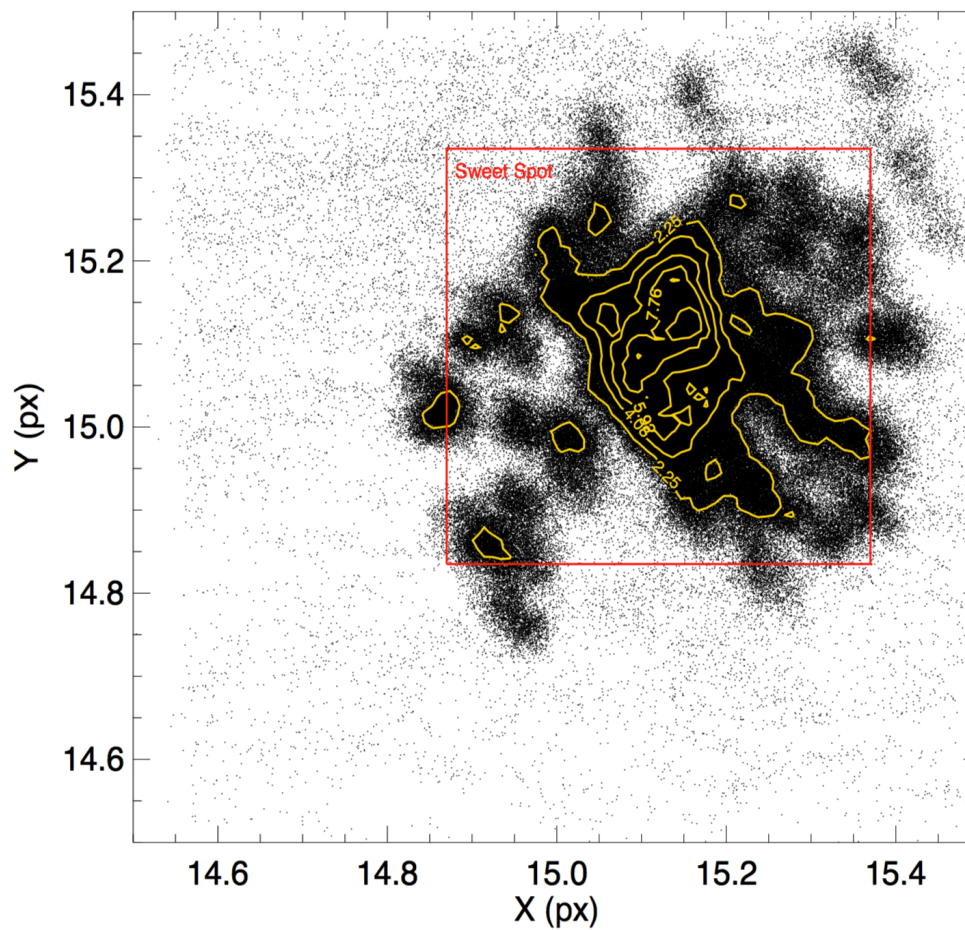


# Mapping a Pixel: Ch 1

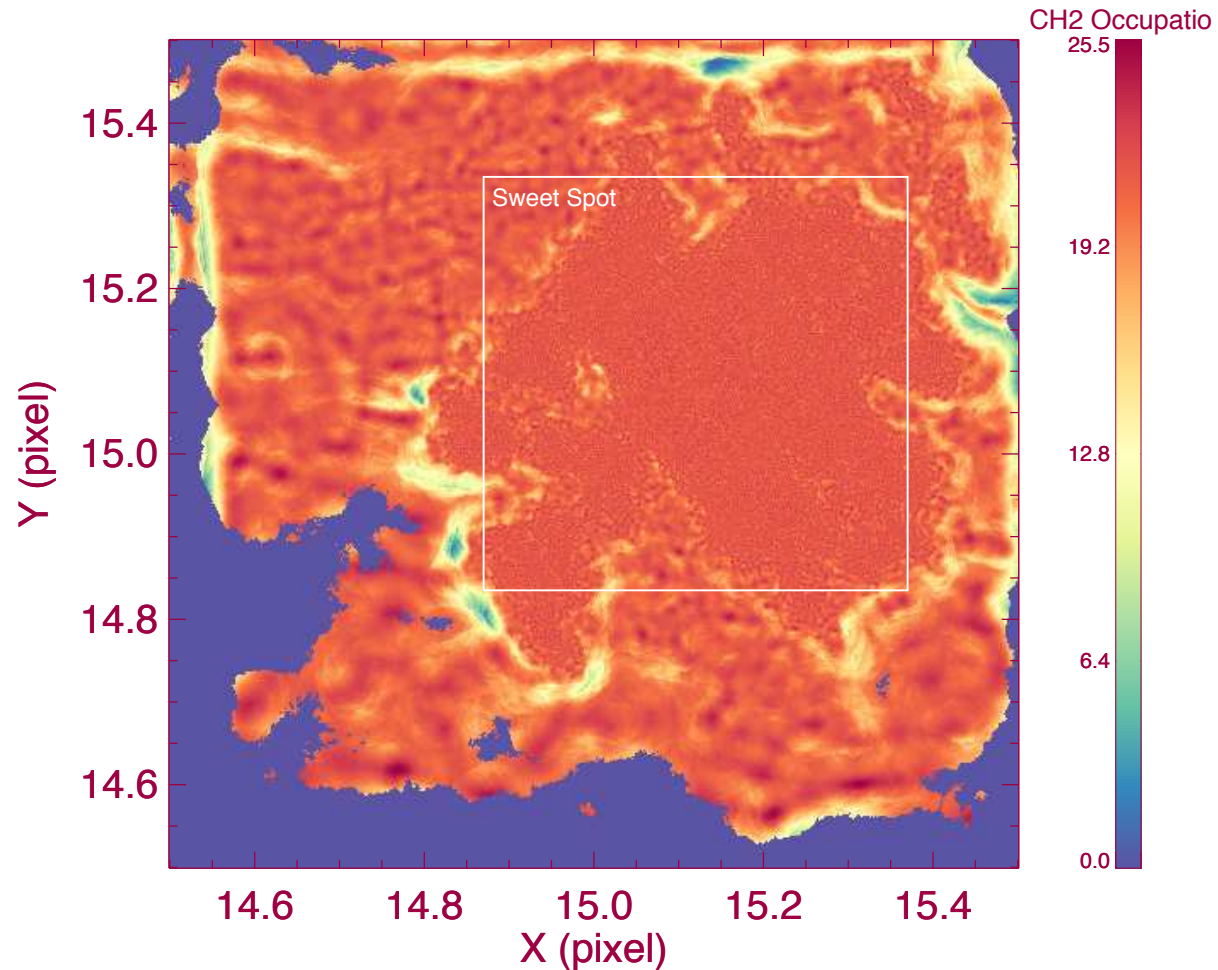


$$\bar{F}(x, y) = \frac{\sum_{i < } f_i K_i}{\sum_{i < } K_i}$$

# Mapping a Pixel: Ch 2



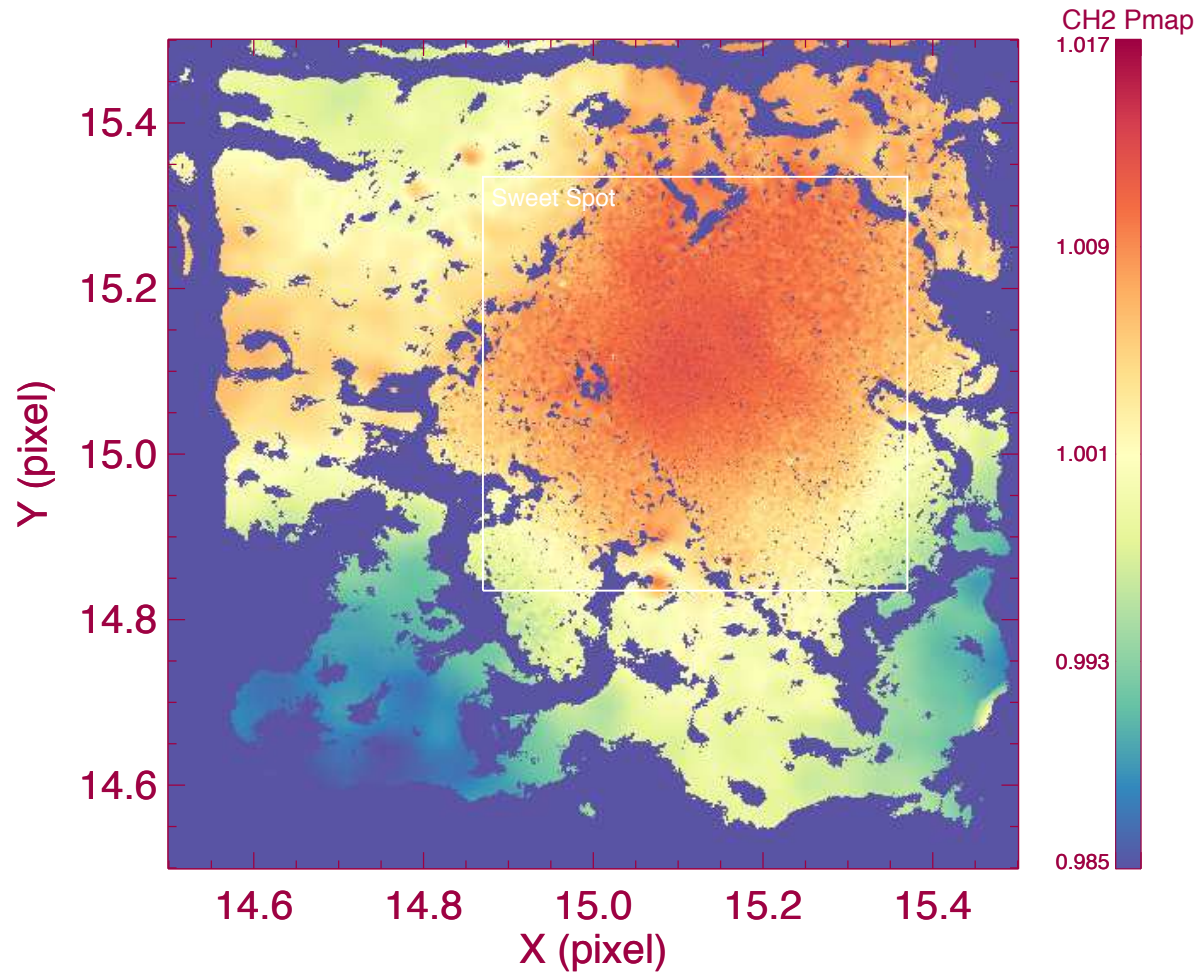
# Mapping a Pixel: CH1



$$O_i(x, y) \equiv \exp \left\{ - \left[ \frac{(x - x_i)^2}{2\delta_x^2} + \frac{(y - y_i)^2}{2\delta_y^2} \right] \right\}$$

$$O(x, y) = \sum_{i <} O_i(x, y)$$

# Mapping a Pixel: Ch 2

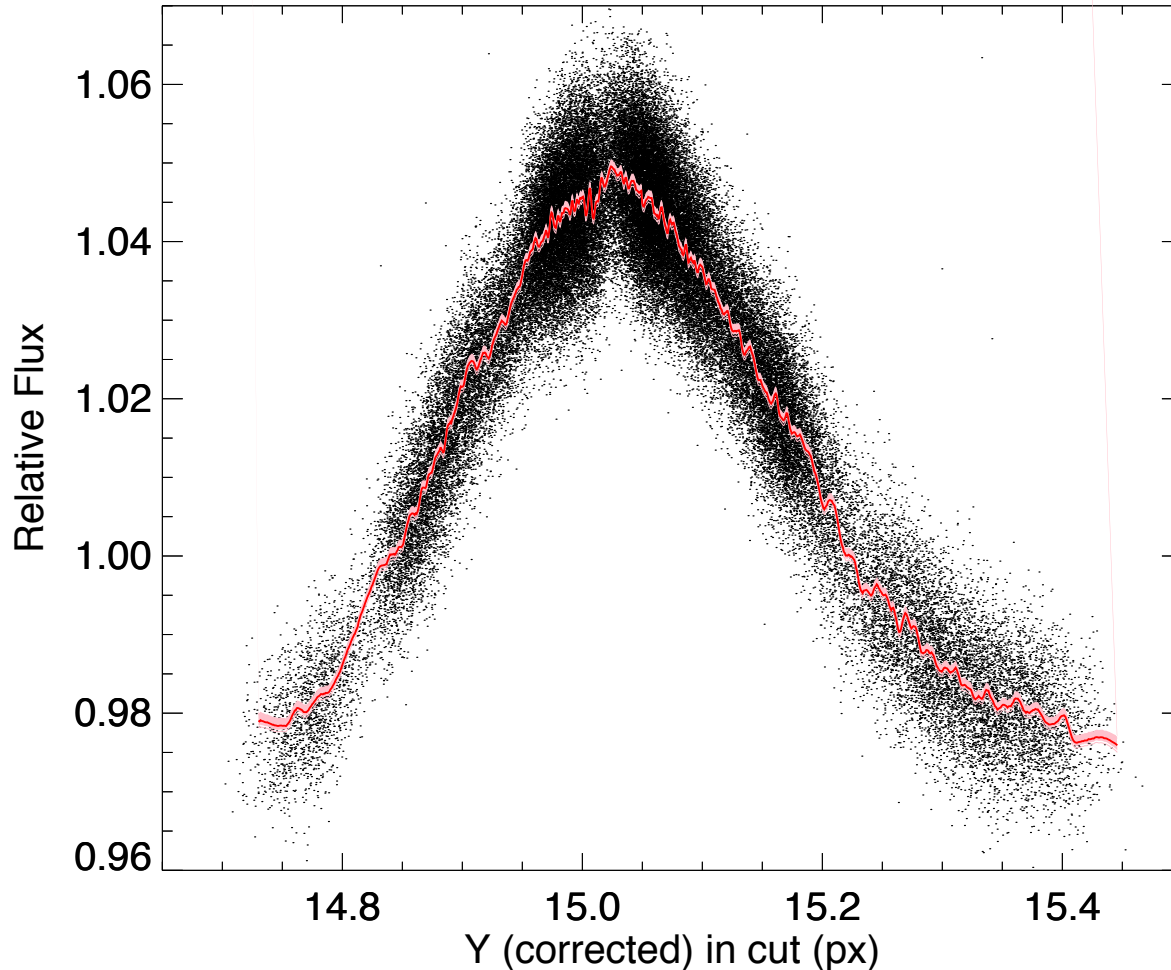


$$\bar{F}(x, y) = \frac{\sum_{i <} f_i K_i}{\sum_{i <} K_i}$$

# Mapping a pixel: Ch 1



Cut:  $15.0 < X < 15.05$



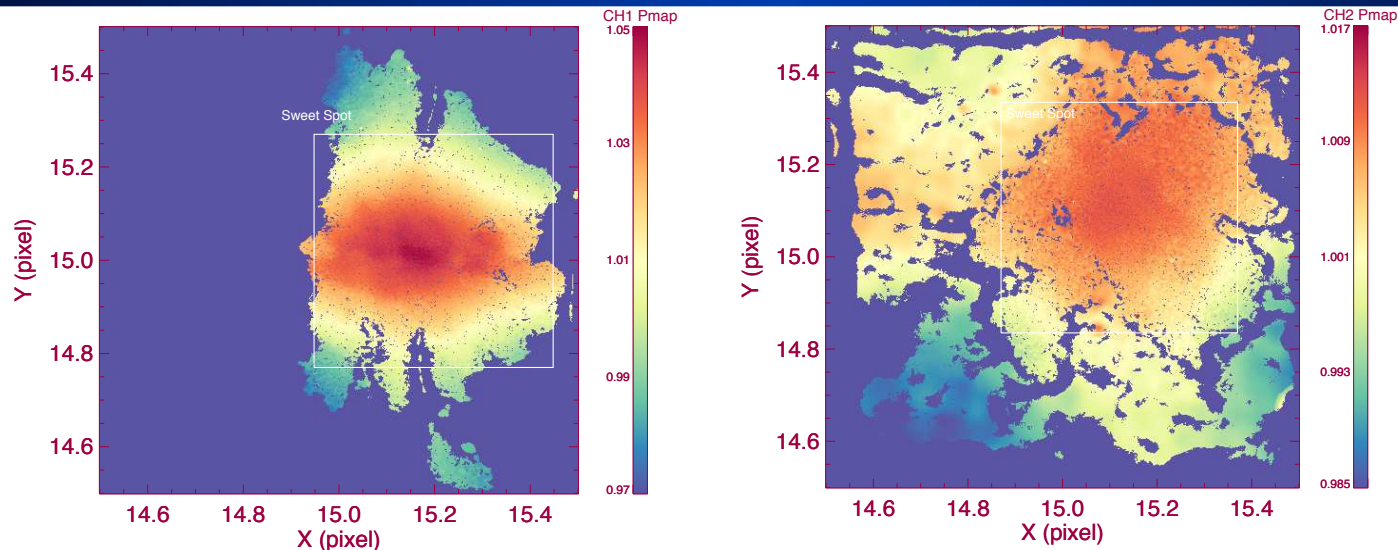
Curve shows regression result for the data shown, in a cut across the y-direction

$$\bar{F}(x, y) = \frac{\sum_{i <} f_i K_i}{\sum_{i <} K_i}$$

Concerns:

- Overfitting
- Time-dependent latent flux

# Correcting Data: New IDL package pmap\_correct



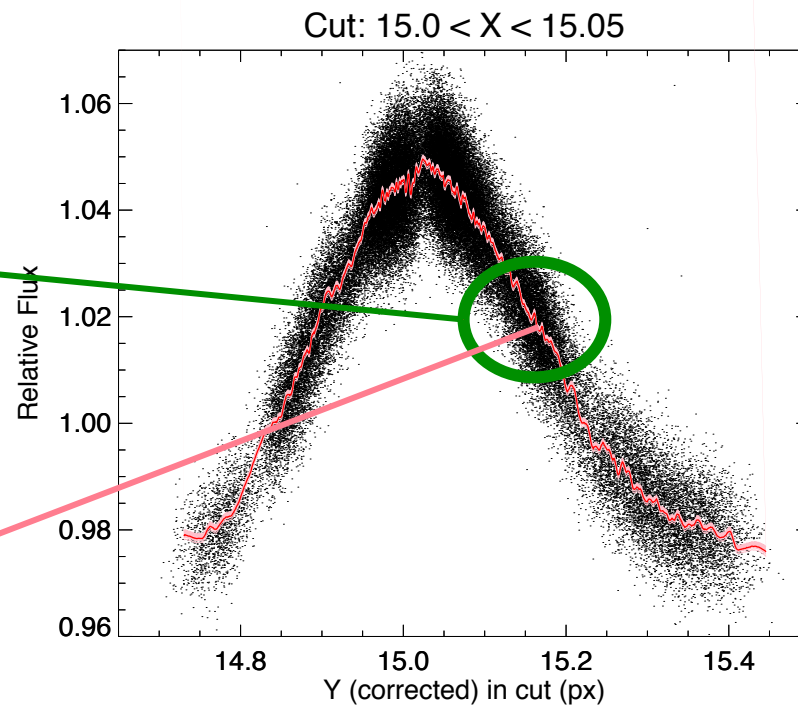
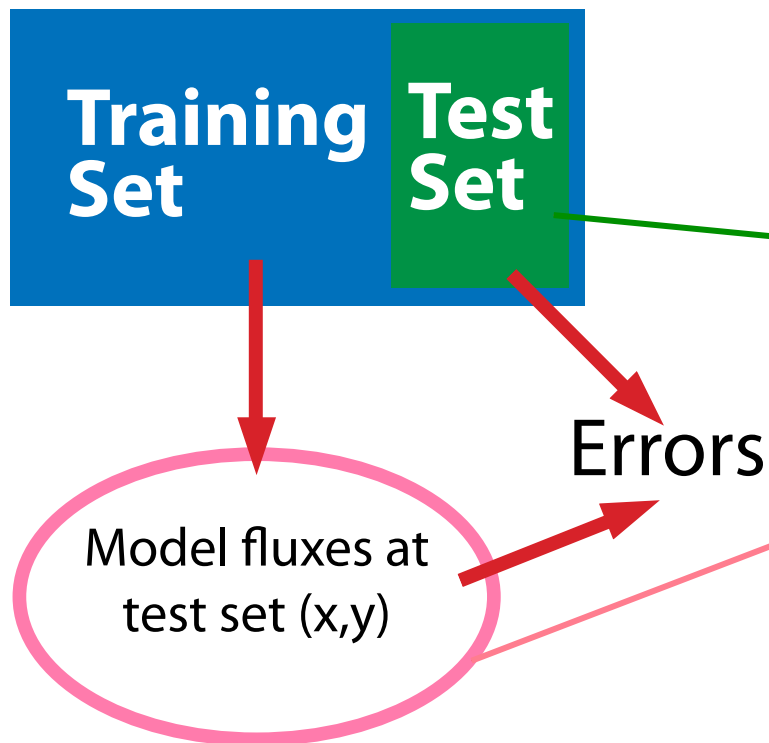
## New code:

- Corrects photometry at  $(x,y)$  by dividing by the regression prediction for normalized flux at  $(x,y)$ , “flattening out” the intra-pixel gain.
- Regression is computed from the NN p-map dataset at the  $(x,y)$  point. Old method interpolated gridded maps (above), suffering from poor resolution and interpolation artifacts.
- Validating with data challenge (Krick).
- Should be available Winter 2015.
- NN algorithm S L O W. Working on ways to speed up using external pre-compiled libraries.

# Extra slides



# Validating the model

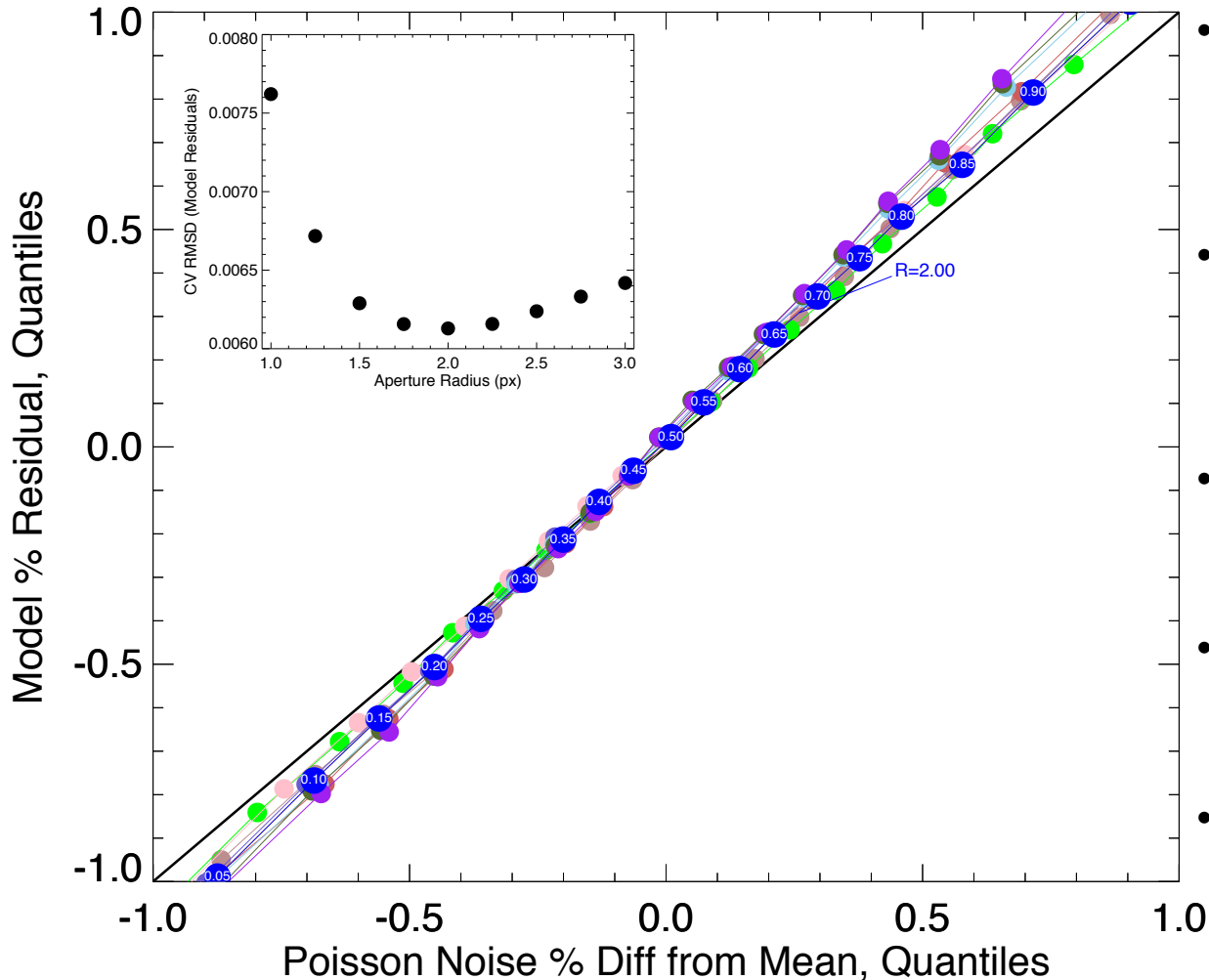




# Do the residuals look like white noise?



CH 1

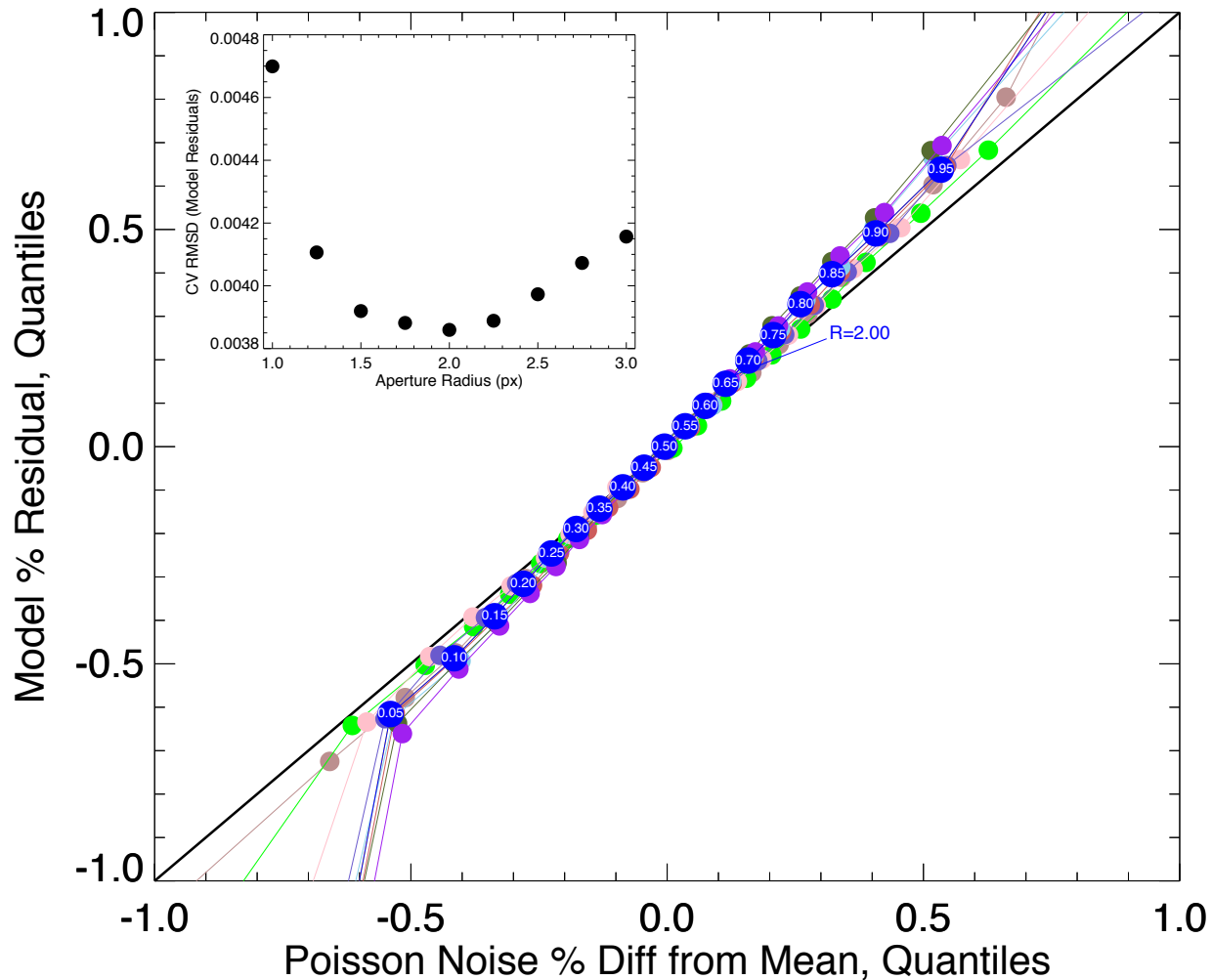


- Q-Q plot is a high S/N technique for comparing distributions.
- Slope > 1: Model distribution is slightly broader than Poisson noise
- 50 pct-ile slightly above line, small bias.
- RMSD/Mean minimum ~0.6% at R=2.0px
- 70% of data within 0.1% of white noise

# Validating the model



CH 2



- Slope > 1: Model distribution is slightly broader than Poisson noise
- 50 pct-ile on line, zero bias.
- RMSD/Mean minimum ~0.38% at R=2.0px
- 70% of data within 0.1% of white noise